

EFFICIENT GENOME SIMILARITY ESTIMATION FOR LEARNING FROM SEQUENCING DATA

Petr Ryšavý, supervised by Filip Železný

Tuesday 3rd October, 2023

IDA, Dept. of Computer Science, FEE, CTU



INTRODUCTION



Estimating Sequence Similarity from Read Sets for Clustering Sequencing Data

[Petr Ryšavý](#) & [Filip Železný](#)

[First Online: 21 September 2016](#)

[Citations](#)

[Notes in Computer Science](#) book series (LNISA, volume 9897)

[Published: 04 August 2018](#)

Estimating Sequence Similarity from Contig Sets

[Petr Ryšavý](#) & [Filip Železný](#)

Conference paper | [First Online: 04 October 2017](#)

938 Accesses | **1** Citations

Part of the [Lecture Notes in Computer Science](#) book series (LNISA, volume 10687)

Estimating sequence similarity from read sets for clustering next-generation sequencing data

[Petr Ryšavý](#) & [Filip Železný](#)

Research | [Open Access](#) | [Published: 27 March 2023](#)

Reference-free phylogeny from sequencing data

[Knowledge Discovery](#) **33**, 1–23 (2019) | [Cite this article](#)

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[BioData Mining](#) **16**, Article number: 13 (2023) | [Cite this article](#)

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circGPA: circRNA functional annotation based on probability-generating functions

[Petr Ryšavý](#), [Jiří Kléma](#) & [Michaela Dostálová Merkerová](#)

[BMC Bioinformatics](#) **23**, Article number: 392 (2022) | [Cite this article](#)

1101 Accesses | **1** Citations | **4** Altmetric | [Metrics](#)

An Algorithm to Calculate the p -value of the Monge-Elkan Distance *

[Petr Ryšavý](#)^[0000–0002–6597–6616] and [Filip Železný](#)^[0000–0001–9780–3376]

Department of Computer Science,
Electrical Engineering, Czech Technical University in Prague,
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Why should we care about genome similarity?



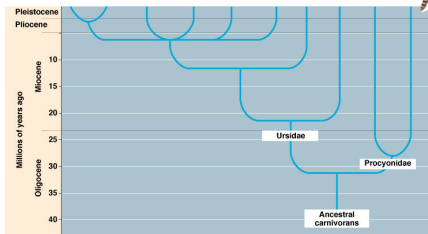
nature
International journal of science

Article | Published: 12 September 1985

A molecular solution to the riddle of the giant panda's phylogeny

Stephen J. O'Brien, William G. Nash, David E. Wildt, Mitchell E. Bush & Raoul E. Benveniste

Nature **317**, 140–144 (12 September 1985) | [Download Citation](#)

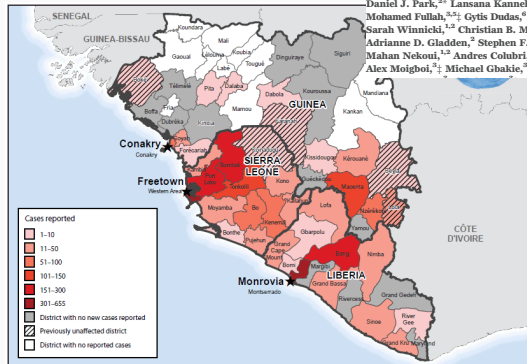


[Reece, Jane B., et al. Campbell biology. No. s 1309. Boston: Pearson, 2014.]



Genomic surveillance elucidates Ebola virus origin and transmission during the 2014 outbreak

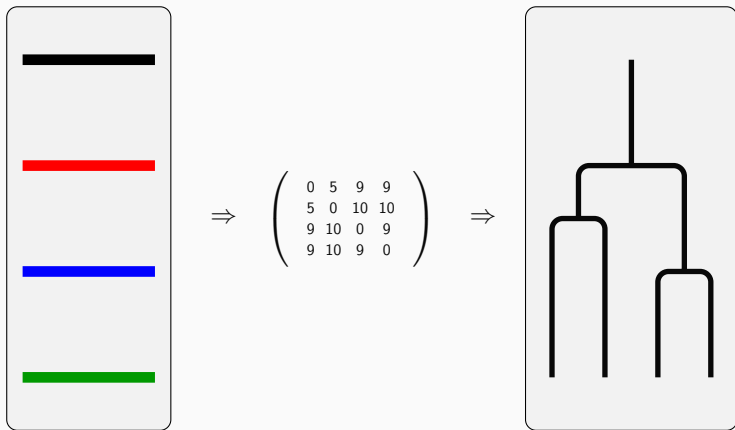
Stephen K. Gire,^{1,2,3} Augustine Goba,^{3,4} Kristian G. Andersen,^{1,2,3} Rachel S. G. Sealton,^{2,4} Daniel J. Park,^{2,5} Lansana Kanneh,² Simbirie Jalloh,³ Mambu Momoh,^{3,5} Mohamed Fullah,^{3,5} Gytis Dudas,⁶ Shirtee Wohl,^{1,2,7} Lina M. Moses,⁸ Nathan L. Yozwiak,^{1,2} Sarah Winnicki,^{1,2} Christian B. Matranga,² Christine M. Malboeuf,² James Qu,² Adrienne D. Gladden,² Stephen F. Schaffner,^{1,2} Xiao Yang,² Pan-Pan Jiang,^{1,2} Mahan Nekoui,^{1,2} Andres Colubri,¹ Moinya Ruth Coomber,² Mbalu Fonnin,⁹ Alex Moigboi,² Michael Gbakie,² Fatima K. Kamara,³ Veronica Tucker,³



[Nolen, Leisha et al. "Incidence of Hansen's Disease — United States, 1994–2011." MMWR. Morbidity and mortality weekly report (2014).]

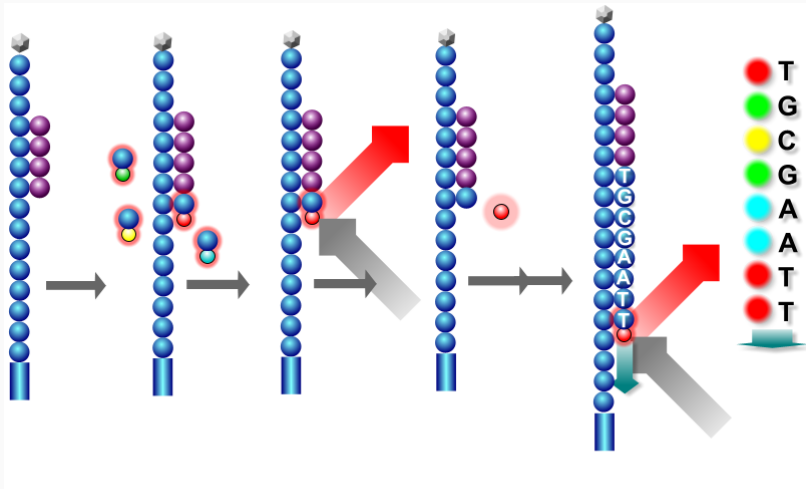


- The only input of hierarchical clustering algorithms is a distance matrix
- This includes UPGMA and neighbor-joining



BACKGROUND - IS IT THAT SIMPLE?

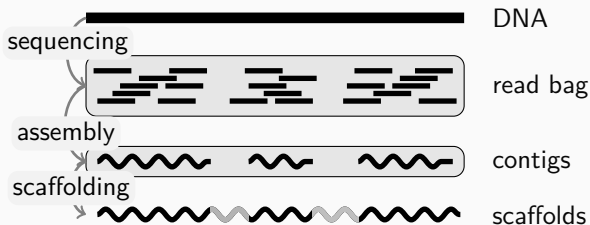
Sequencing by synthesis



[By Abizar Lakdawalla, CC BY-SA 3.0, https://en.wikipedia.org/wiki/File:Sequencing_by_synthesis_Reversible_terminators.png]

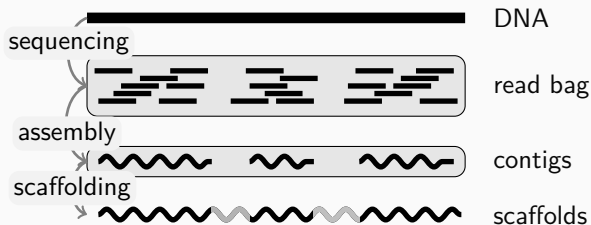


- Product of sequencing is not a long sequence, but short substrings called **reads**
- Reads have length of 10s to 100s of symbols
- Sequence AGGCTGGA is represented by set {AGGC, TGGA, GCT}.





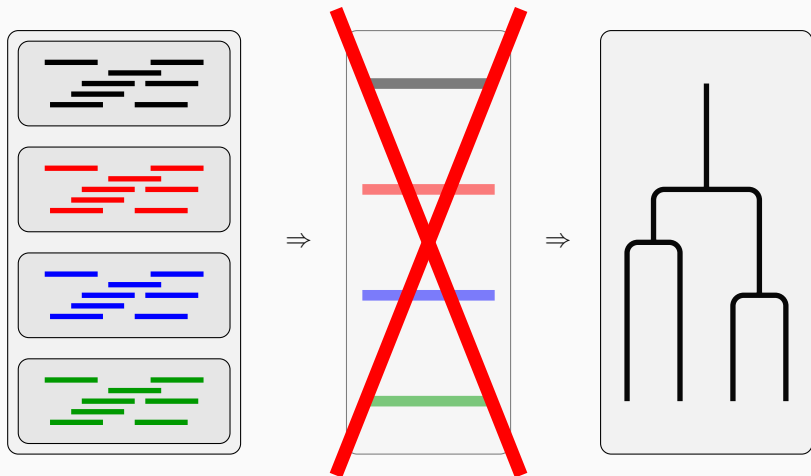
- Assembly does not produce a single putative sequence, but several **contigs**
- Process of scaffolding and gap filling requires some additional wet-lab work
- Contigs are approximate substrings with unknown locations and orientation



Our approach - skip assembly.



- The goal is to build a dendrogram directly from the read sets



- Assumption:** no reference sequence known



- Originally designed to avoid alignment step for genome comparison
- Genome broken into k -mers
- Some approaches work with read data

Comin and Schind *BMC Bioinformatics* 2014, **15**(Suppl 9):S1
<http://www.biomedcentral.com/1471-2105/15/S9/S1>



PROCEEDINGS

Open Access

Assembly-free genome comparison based on next-generation sequencing reads and variable length patterns

Matteo Comin*, Michele Schind

From RECOMB-Seq: Fourth Annual RECOMB Satellite Workshop on Massively Parallel Sequencing
Pittsburgh, PA, USA. 31 March - 05 April 2014

BRIEFINGS IN BIOINFORMATICS, VOL 15, NO 2, 343-353
Advance Access published on 23 September 2013

[doi:10.1093/bib/bbt067](https://doi.org/10.1093/bib/bbt067)

New developments of alignment-free sequence comparison: measures, statistics and next-generation sequencing

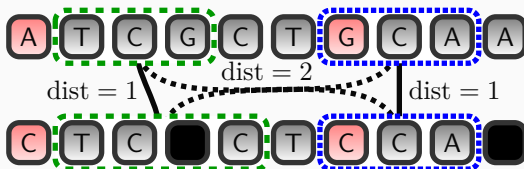
Kai Song, Jie Ren, Gesine Reinert, Minghua Deng, Michael S. Waterman and Fengzhu Sun

Submitted: 28th May 2013; Received (in revised form): 25th July 2013

DISTANCE FUNCTION DESIGN



- Our approach is based on the Monge-Elkan distance known from databases
- For each read from a read set, we find the least distant read in the second read set



- Then we average over the read pairs

Estimating Sequence Similarity from Read Sets for Clustering Sequencing Data

[Petr Ryšavý](#) & [Filip Železný](#)

Conference paper | [First Online: 21 September 2016](#)

1631 Accesses | **4** Citations

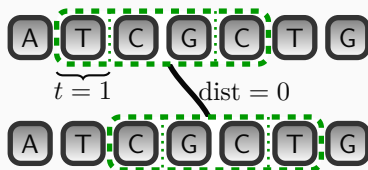
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- Our measure should be symmetric
- The Monge-Elkan distance has upper bound l
- Bring distance to proper scale



- Special treatment of leading and trailing gaps
- They may be caused by random positions of the reads



- Modification to edit distance

IMPROVEMENTS



- Coverage c around 2 provides results that are good enough.
- For high coverage data, downsample to $c = 2$.

[Published: 04 August 2018](#)

Estimating sequence similarity from read sets for clustering next-generation sequencing data

[Petr Ryšavý](#) ✉ & [Filip Železný](#)

[Data Mining and Knowledge Discovery](#) **33**, 1–23 (2019) | [Cite this article](#)

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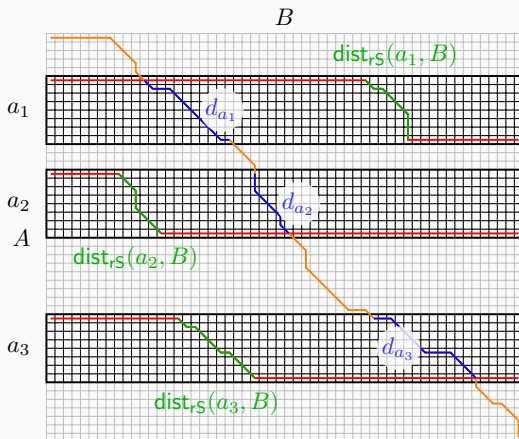


- We do not need an exact minimum in the Monge-Elkan distance.
- We use embedding to identify good candidates.
- q -gram profile is vector of counts of all possible q -grams, i.e. strings from Σ^q .
- q -gram distance of two strings is the Manhattan distance of their q -gram profiles.
- Inspiration by BLAST and dictionary search, $q = 3$.
- We evaluate edit distance only on reads minimizing the q -gram distance.
- q -gram distance is LB on edit distance.

THEORETICAL ANALYSES



- If we use a read bag and a sequence, a Monge-Elkan-alike distance serves as a lower-bound





- We developed a p -value algorithm for the Monge-Elkan distance
- Based on generating polynomials, combinatorics, and improved with FFT

An Algorithm to Calculate the p -value of the Monge-Elkan Distance *

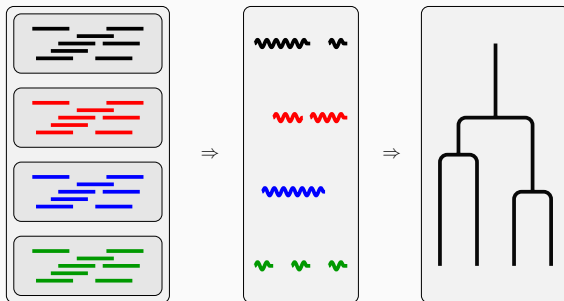
Petr Ryšavý^[0000-0002-6597-6616] and Filip Železný^[0000-0001-9780-3376]

Department of Computer Science,
Faculty of Electrical Engineering, Czech Technical University in Prague,
Prague, Czech Republic
`{petr.rysavý,zelezny}@fel.cvut.cz`

USING CONTIG-SETS



- Do not skip the assembly; do only the easy parts.



Estimating Sequence Similarity from Contig Sets

[Petr Ryšavý](#) ✉ & [Filip Železný](#)

Conference paper | [First Online: 04 October 2017](#)

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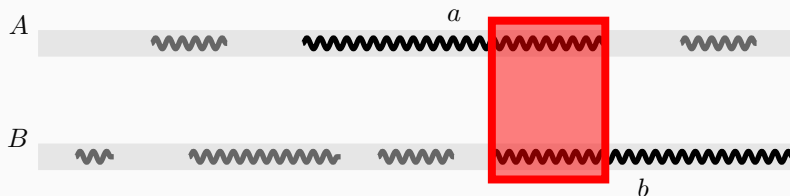
1) Estimating overlaps for contig pairs



- Consider two contigs α and β and assume they overlap in the optimal alignment
- Select overlap that minimizes the post-normalized edit distance

$$\overline{\text{dist}}(\alpha, \beta) = \frac{\text{dist}(\alpha, \beta)}{\max\{|\alpha|, |\beta|\}}. \quad (1)$$

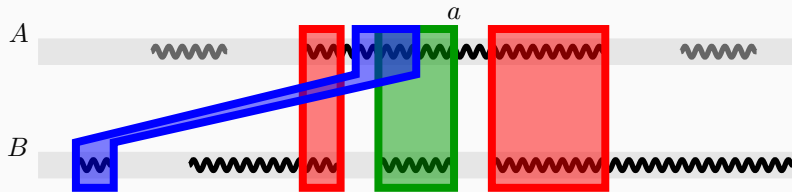
- Heuristic approach based on modification of Smith-Waterman algorithm



2) Estimating overlaps for contig sets



- For one contig, we have overlaps with the other contig set
- Select non-overlapping regions that maximize the total value (post-normalized edit distance)
- Reduction to *weighted interval scheduling problem*



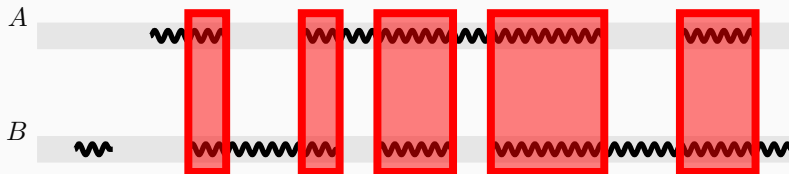
3) Combining the Results



- Sum distances of overlap pairs

$$d(C_A, C_B) = \sum_{(c,d) \in \text{overlap}(C_A, C_B)} \text{dist}(c, d).$$

- The sum does not capture contig size w.r.t. genome size



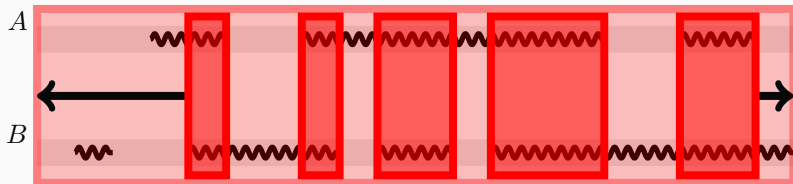
3) Combining the Results



- Normalize
- Divide by maximum possible distance of all overlaps ...
- ... and multiply by genome maximum distance

$$d(C_A, C_B) = \frac{\sum_{(c,d) \in \text{overlap}(C_A, C_B)} \text{dist}(c, d)}{\sum_{(c,d) \in \text{overlap}(C_A, C_B)} \max\{|c|, |d|\}} \cdot \frac{l \max\{|R_A|, |R_B|\}}{\alpha}.$$

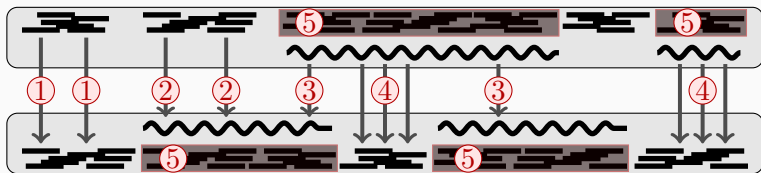
- Finally, make the resulting measure symmetric ...



COMBINATION OF THE MEASURES



- Requires dealing with many read/contig combination pairs



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Reference-free phylogeny from sequencing data

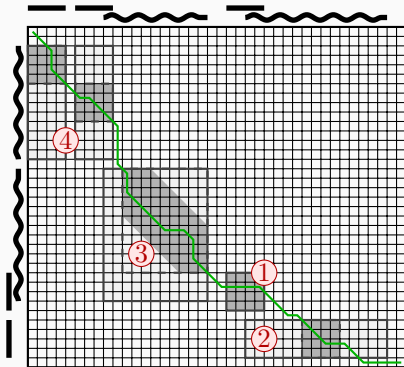
[Petr Ryšavý](#) ✉ & [Filip Železný](#)

BioData Mining **16**, Article number: 13 (2023) | [Cite this article](#)

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- Ideally, the algorithm should calculate an alignment only around the optimal alignment path



EXPERIMENTAL RESULTS



- Two real-world and three artificial datasets
- Original DNA sequences used as a reference (if available)
- Two clustering algorithms (Neighbor-joining and UPGMA)
- Comparison using 5 common de novo assemblers (ABYSS, edena, SSAKE, SPADes, velvet)
- Comparison with alignment-free measures (8 d -type statistics, Mash, co-Phylog)



- **time** (assembly time, distance matrix time, clustering time)
- **Pearson's correlation coefficient** measuring the similarity of the distance matrix to the reference one
- **Fowlkes-Mallows index** measuring similarity of the clusterings
- Averaging over c and l values.



• Pearson's correlation between distance matrices is close to one

Table 4 Runtime, Pearson's correlation coefficient between distance matrices and Fowlkes-Mallows index for $k = 4$ and $k = 8$. The 'reference' method calculates distances from the original sequences. We show only assembly algorithm that gave the highest correlation, the best d -type method, and the better algorithm of pairs MES/MESS, MESSG/MESSGM, and MESSGq/MESSGMq.

Dataset	method	finished	<u>assem.</u> <u>ms</u>	<u>distances</u> <u>ms</u>	<u>UPGMA</u> <u>ms</u>	<u>NJ</u> <u>ms</u>	corr.	<u>UPGMA</u> <u>B₄</u>	<u>UPGMA</u> <u>B₈</u>	<u>NJ</u> <u>B₄</u>	<u>NJ</u> <u>B₈</u>
Influenza	reference	112/112	0	3,991	4.59	3.25	1	1	1	1	1
	$\max(R_A , R_B)$	112/112	0	337	1.08	3.25	.801	.67	.319	.658	.319
	Dist _{MESS}	112/112	0	829,411	0.24	0.26	.945	1	.866	1	.84
	Dist _{MESSG}	104/112	0	986,757	0.13	0.36	.981	.995	1	.998	.993
	Dist _{MESSGq}	112/112	0	49,260	0.09	0.53	.971	.999	.992	.999	.985
	Mash	112/112	0	117	1.53	8.59	.679	.476	.575	.438	.61
	d_2^2	111/112	0	352	4.86	3.36	.837	.378	.712	.403	.898
	SPAdes	43/112	12,230	4,644	0.33	1.07	.928	.965	.752	.94	.781
Various	reference	112/112	0	59,602	5.21	3.40	1	1	1	1	1
	$\max(R_A , R_B)$	112/112	0	596	1.95	2.35	.907	.671	.655	.846	.924
	Dist _{MESS}	76/112	0	1,302,199	0.36	0.53	.93	.627	.804	.873	.933
	Dist _{MESSG}	70/112	0	1,575,721	0.29	0.64	.933	.621	.884	.932	.93
	Dist _{MESSGMq}	110/112	0	570,361	0.29	0.79	.927	.657	.771	.842	.972
	Mash	112/112	0	238	4.88	11.26	.498	.408	.267	.428	.326
	d_2^2	109/112	0	689	4.84	19.32	.442	.378	.189	.453	.317
	SPAdes	34/112	18,675	177,821	0.21	0.79	.942	.698	.91	.961	.949
Hepatitis	reference	9/9	0	1,759,470	25.00	44.44	1	1	1	1	1
	$\max(R_A , R_B)$	9/9	0	18,913	7.11	14.00	.181	.553	.368	.724	.828
	Dist _{MES}	9/9	0	10,994,207	1.11	3.56	.833	1	.952	1	.961
	Dist _{MESSGM}	9/9	0	20,489,458	4.78	3.78	.965	.994	.946	1	.903
	Dist _{MESSGMq}	9/9	0	697,464	1.56	5.78	.9	.915	.947	1	.944
	Mash	9/9	0	3,788	23.00	141.33	.967	.964	.966	1	.918
	d_2^2	9/9	0	26,301	47.11	397.00	.973	.984	.96	1	.87
	Velvet	9/9	17,774	2,398,724	1.00	3.67	.782	.803	.846	.964	.847
Chromosomes	reference	1/1	0	653,909	7.00	4.00	1	1	1	1	1
	$\max(R_A , R_B)$	1/1	0	1,247	1.00	1.00	.331	.64	.404	.613	.298
	Dist _{MES}	1/1	0	10,645,321	1.00	0.00	.886	.42	.263	.596	.276
	Dist _{MESSGα}	1/1	0	20,713,067	1.00	1.00	.848	.408	.227	.585	.26
	Dist _{MESSGqα}	1/1	0	178,840	1.00	1.00	.841	.673	.301	.9	.262
	Mash	1/1	0	261	1.00	4.00	.33	.588	.307	.599	.382
	d_2^2	1/1	0	1,768	0.00	2.00	.302	.503	.328	.805	.303
	SSAKE α	1/1	46,853	55,131	1.00	1.00	.652	.528	.17	.805	.255



Exact evaluation of the Monge-Elkan distance is too slow for real-world

Table 4 Runtime, Pearson's correlation coefficient between distance matrices and Fowlkes-Mallows index for $k = 4$ and $k = 8$. The 'reference' method calculates distances from the original sequences. We show only algorithm that gave the highest correlation, the best d -type method, and the better algorithm of pairs MES/MESS, MESSG/MESSGM, and MESSGq/MESSGMq.

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Influenza	reference	112/112	0	3,991	4.59	3.25	1	1	1	1	1
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	d_2^*	9/9	0	26,301	47.11	397.00	.973	.984	.96	1	.87
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	SSAKEα	1/1	46,853	55,131	1.00	1.00	.652	.528	.17	.805	.255



- Embedding and scaling puts runtime between assembly and alignment-free approaches

Table 1 Runtime on “E. coli” dataset. Assembly time (without distance matrix calculation) on the same dataset is 18,844 s (ABYSS), 18,606 s (Edena), 33,545 s (SPAdes), and 17,701 s (Velvet).

Method	Time (in seconds)
Dist _{MESSG(M)} _{qα}	11,073
co-phylog	583
Mash	480
d_2	3,221
d_2^*	3,235
d_2^q	3,228
d_2^{q*}	3,225
D_2	3,235
D_2^*	3,301
D_2^q	3,224
D_2^{q*}	3,227



- Our approach requires lower coverage than assembly

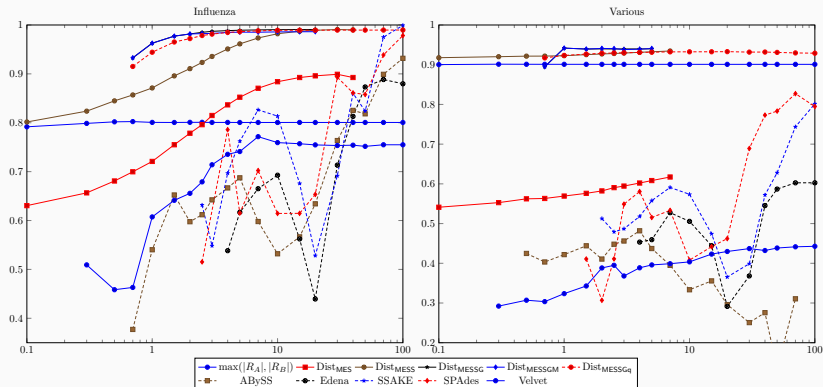


Figure 2: Plot of average Pearson's correlation coefficient for several choices of coverage values.



- Our approach works better for short reads than assembly

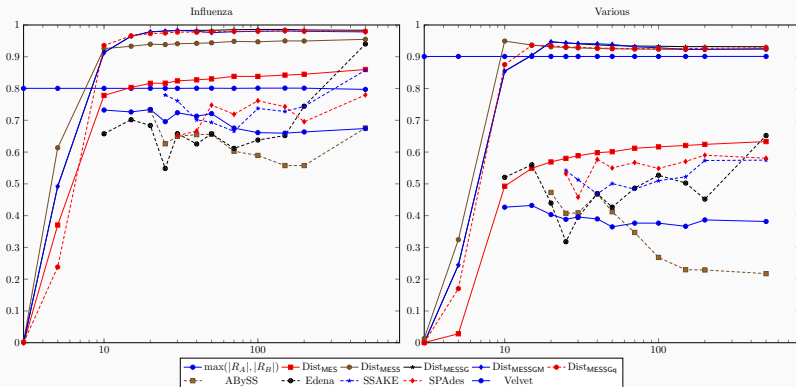


Figure 3: Plot of average Pearson's correlation coefficient for several choices of read length.



- We have seen three methods for estimating sequence similarity from read/contig sets or both
- Only single approximation step
- Adapts advantages of both alignment-free approaches and alignment similarity
- Due to low coverage requirements and small read length requirements, possible applications might include MiSeq, or as part of supertree methods
- Applicable to other similarity-based learning methods, as k -NNs

CIRCULAR RNAs

Research | [Open Access](#) | [Published: 27 September 2022](#)

circGPA: circRNA functional annotation based on probability-generating functions

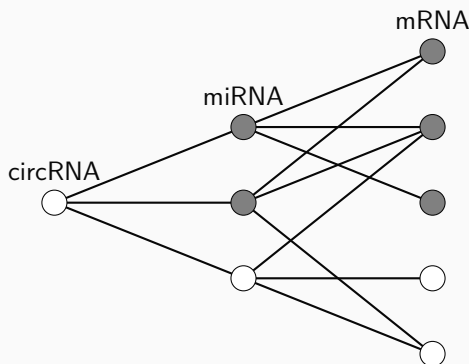
[Petr Ryšavý](#) , [Jiří Kléma](#) & [Michaela Dostálová Merkerová](#)

BMC Bioinformatics **23**, Article number: 392 (2022) | [Cite this article](#)

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- In a second project, we focused on annotation of circular RNAs with annotation terms (as gene ontology terms)
- Today, the function of many circRNAs remains unknown
- An automatic tool to annotate circRNAs needed
- Annotation of miRNAs and mRNAs available
- Interaction graph is known (miRNA silencing and circRNA sponging)



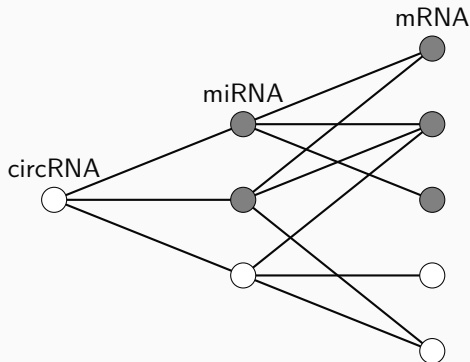


- $\vec{a}^{\mu,c} = (1, 1, 1)$

- $\mathbf{A}^{m,\mu} = \begin{pmatrix} 0 & 1 & 1 \\ 1 & 1 & 1 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \\ 1 & 1 & 0 \end{pmatrix}$

- $\vec{g}^{\mu} = (0, 1, 1)$

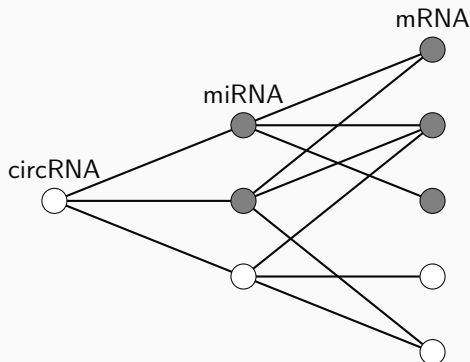
- $\vec{g}^m = (1, 1, 1, 0, 0)$



ANNOTATION ALGORITHM

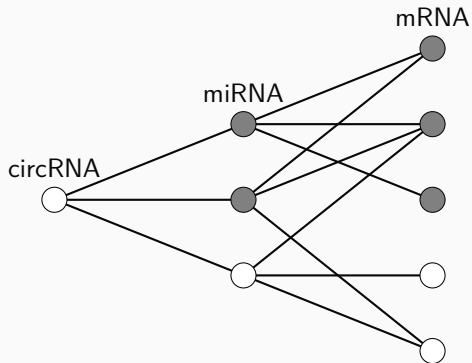


- Problems are independent for different circRNAs and different terms
- Guilt by association principle
- We can count the number of paths from the circRNA that end in a miRNA/mRNA annotated with the term





$$\vec{a}^{\mu,c} \cdot \vec{g}^{\mu} + \mathbf{A}^{m,\mu} \vec{a}^{\mu,c} \cdot \vec{g}^m$$





- More frequent terms have a higher statistic
- We can solve this bias by using the p -value
- Calculate the probability that we get a higher statistic for the same size term by chance
- Traditionally solved by generating random subsets and calculating the statistic (Barnard's Monte-Carlo sampling)



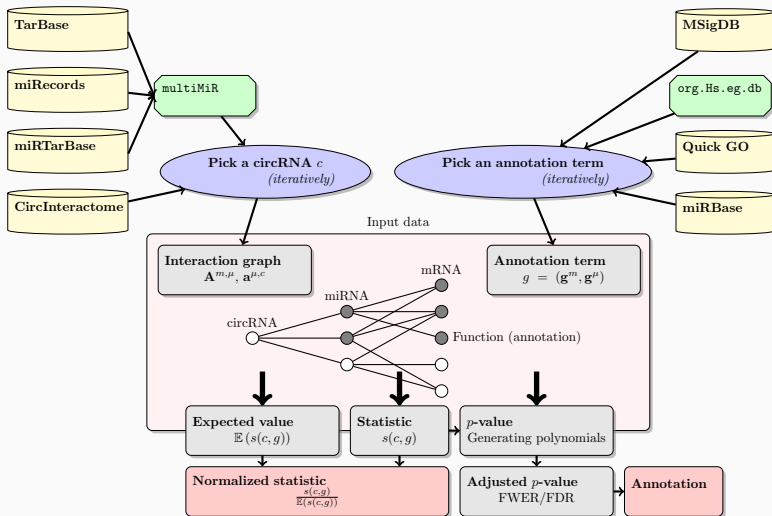
- Using a generating polynomial
- Imagine tossing a dice with sides $(1, 2, 3, 3, 3, 4)$, then the generating polynomial is

$$x + x^2 + 3x^3 + x^4$$

- Tossing this dice twice gives

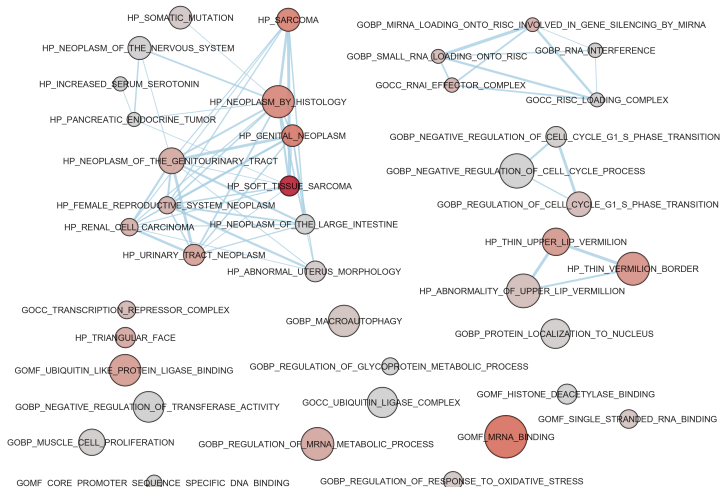
$$(x + x^2 + 3x^3 + x^4)^2 = x^2 + 2x^3 + 7x^4 + 8x^5 + 11x^6 + 6x^7 + x^8$$

The complete pipeline

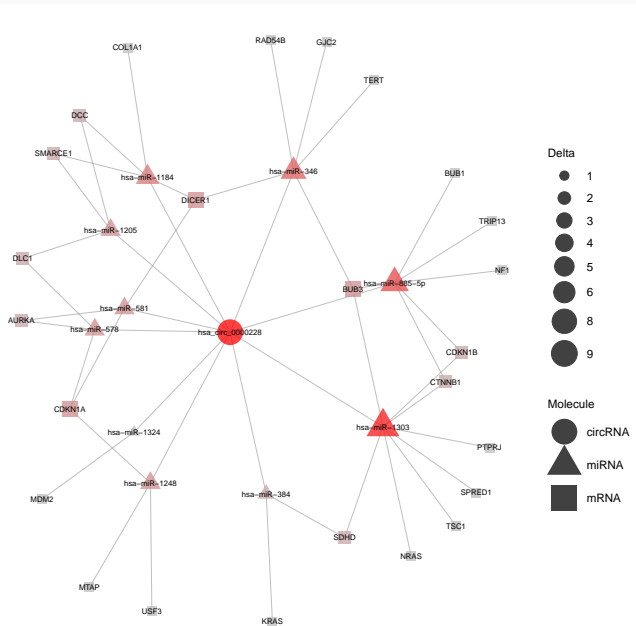


RESULTS

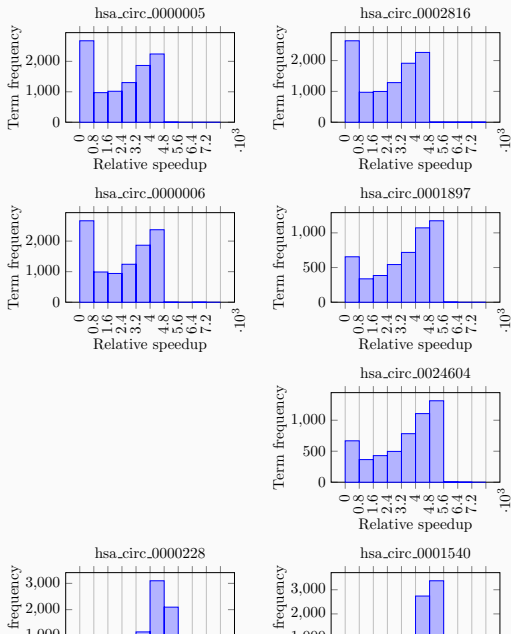
A sample output - annotation of hsa_circ_0000228



A sample output - influence of interacting RNAs



Evaluation - faster than the Monte-Carlo sampling



CONCLUSION - WORK IN PROGRESS



- The edges can be weighted by co-expression
- The vertices can be weighted by the log-fold changes
- This way, we incorporate the expression matrix

Another problem:

- The tool can be used to mine circRNA-disease associations

Estimating Sequence Similarity from Read Sets for Clustering Sequencing Data

Petr Ryšavý✉ & Filip Železný

First Online: 21 September 2016

Citations

Notes in Computer Science book series (LNISA, volume 9897)

Published: 04 August 2018

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Conference paper | First Online: 04 October 2017

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An Algorithm to Calculate the p -value of the Monge-Elkan Distance *

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TIME FOR QUESTIONS!



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